



Performance of the Muon Identification at LHCb

The LHCb MuonID group [†]

Abstract

The performance of the muon identification in LHCb is extracted from the data using muons and hadrons produced in the $J/\psi \rightarrow \mu^+\mu^-$, $\Lambda^0 \rightarrow p\pi$ and $D^{*+} \rightarrow \pi^+D^0(K^-\pi^+)$ decays. The muon identification procedure is based on the pattern of the hits in the muon chambers. A momentum dependent binary requirement is used to reduce the probability of hadrons to be misidentified as muons to the 1% level, keeping the muon efficiency in the range 95-98%. Then a likelihood is built for the muon and non-muon hypotheses. Adding a requirement on this likelihood that provides a total muon efficiency at the level of 93%, the hadron misidentification probabilities are below 0.6%.

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1 Introduction

LHCb [1] is a dedicated heavy flavour experiment, designed to exploit the high $pp \rightarrow c\bar{c}$ and $pp \rightarrow b\bar{b}$ cross-sections at the LHC in order to perform precision measurements of CP violation and rare decays. Muons are present in the final state of many of the key decays, sensitive to new physics. Moreover, they play a crucial role in the determination of the flavor tagging of the neutral B mesons and are also present in the signatures of interesting electroweak and strong processes. The muon identification procedure must provide high muon efficiency while keeping the incorrect identification probability of light hadrons as muons (misidentification probabilities) at the lowest possible level. The pion misidentification is one of the major sources of combinatoric background for decays with muons in the final state. It is also important to keep the other hadron misidentification probabilities at low levels so that rare decays can be separated from more abundant hadronic decays with similar or identical topology.

This paper presents the performance of the muon identification in LHCb, obtained from the data taken in 2011, corresponding to approximately 1 fb^{-1} . In Section 2, a brief description of the LHCb spectrometer and the muon detection system is given. The muon identification algorithm is discussed in Section 3. The method used to extract the muon efficiency and the misidentification probability from data is explained in Section 4. Finally, the performance results are presented in Section 5, followed by the conclusions in Section 6.

2 The LHCb experiment and the muon system

The LHCb detector [1] is a single-arm forward spectrometer. A vertex locator (VELO) determines with high precision the positions of the vertices of pp collisions (PVs) and the decay vertices of long-lived particles. The tracking system includes a silicon strip detector located in front of a dipole magnet with an integrated field of around 4 Tm, and a combination of silicon strip detectors and straw drift chambers placed behind the magnet, allowing the momentum determination of charged particles with a resolution of $\sigma_p/p \sim 0.4(0.6)\%$ at a momentum scale of $3(100)\text{ GeV}/c$. Charged hadron identification is achieved with two ring-imaging Cherenkov (RICH) detectors. The calorimeter system consists of a scintillator pad detector, a preshower, an electromagnetic calorimeter and a hadronic calorimeter. It identifies high transverse energy hadron, electron and photon candidates and provides information for the trigger.

The muon system [2] is composed of five stations (M1-M5) of rectangular shape, placed along the beam axis. As shown in Fig. 1, stations M2 to M5 are placed downstream the calorimeters and are interleaved with iron absorbers 80 cm thick to select penetrating muons. Station M1 is located in front of the calorimeters and is used to improve the transverse momentum measurement in the first level hardware trigger. The total absorber thickness in front of station M2, including the calorimeters, is approximately 6.6 interaction lengths. The major part of the system is equipped with multi-wire proportional chambers (MWPC) with Ar/CO₂/CF₄(40:55:5) as gas mixture. Only

LHCb Event Display

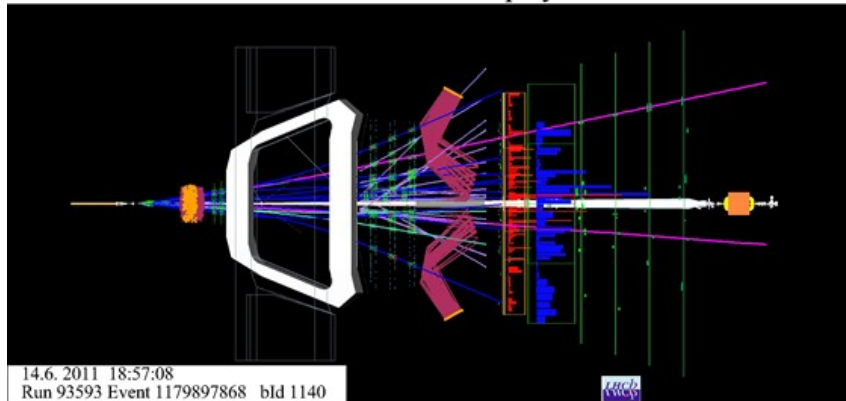


Figure 1: Schematic view of the LHCb experiment, displaying one event recorded in 2011, where 2 muons are identified (purple tracks). This is one of the best $B_s^0 \rightarrow \mu^+ \mu^-$ candidates selected from the 2011 data [3]. The muon stations are seen as the five green vertical lines, the second one placed just after the calorimeters, shown as the rectangles with red and blue bars representing the energy deposition along the direction transverse to the beam.

41 the inner part of the first station is instrumented with triple-GEM detectors filled with
 42 Ar/CO₂/CF₄(45:15:40).

43 The chambers are positioned to provide with their sensitive area a hermetic geometric
 44 acceptance to high momentum particles coming from the interaction point. In addi-
 45 tion, the chambers of different stations form projective towers pointing to the interac-
 46 tion point. The detectors provide digital space point measurements of the particle trajectories,
 47 supplying information to the trigger processor and to the data acquisition (DAQ). The
 48 information is obtained by partitioning the detector into rectangular logical pads whose
 49 dimensions define the x, y resolution in the plane perpendicular to the beam axis. Each
 50 station is divided into four regions, R1 to R4 with increasing distance from the beam
 51 axis. The linear dimensions of the regions R1, R2, R3, R4, and their segmentation scale
 52 in the ratio 1:2:4:8. Each muon station is designed to perform with an efficiency above
 53 99% in a 20 ns time window with a noise rate below 1 kHz per physical channel, which
 54 was achieved during operation, as described in [2].

55 The muon system provides information for the selection of high transverse momentum
 56 muons at the trigger level and for the offline muon identification. This document refers
 57 to the latter procedure, which uses only the information from the 4 stations located after
 58 the calorimeters. The muon identification in the trigger system is described in [4].

59 **3 The muon identification procedure**

60 The muon identification strategy in the LHCb experiment can be divided in two steps:

- 61 • a loose binary selection of muon candidates based on the penetration of the muons
62 through the calorimeters and iron filters, which provides high efficiency while reduc-
63 ing the rate of hadrons to the percent level;
- 64 • computation of a likelihood for the muon and non-muon hypotheses, based on the
65 pattern of hits around the extrapolation to the different muon stations of the charged
66 particles trajectories reconstructed with high precision in the tracking system.

67 3.1 IsMuon binary selection

The binary selection, hereafter denominated IsMuon (true for tracks identified as muons and false otherwise), is defined according to the number of stations where a hit is found within a field of interest (FOI) defined around the track extrapolation. The number of stations required to be fired is a function of track momentum (p), as shown in Table 1. The sizes of the fields of interest also depend on the particle momentum and are defined according to the expected multiple scattering suffered by a muon when traversing the material. The FOI are parameterized separately for the 4 regions of the 4 different stations downstream the calorimeter in both x and y directions according to:

$$\text{FOI} = a + b * \exp(-cp).$$

68 The parameters a , b and c have been determined using muons from a full detector Monte
69 Carlo simulation [5].

Momentum range	Muon stations
$3 \text{ GeV}/c < p < 6 \text{ GeV}/c$	M2 and M3
$6 \text{ GeV}/c < p < 10 \text{ GeV}/c$	M2 and M3 and (M4 or M5)
$p > 10 \text{ GeV}/c$	M2 and M3 and M4 and M5)

Table 1: Muon stations required to trigger the IsMuon decision as a function of momentum range.

70 For tracks passing the IsMuon requirement, the muon identification can be further
71 improved by a selection based on the logarithm of the ratio between the likelihoods for
72 the muon and non-muon hypotheses (muDLL).

73 3.2 Muon and non-muon likelihoods

74 The likelihoods are computed as the cumulative probability distributions of the average
75 squared distance significance D^2 of the hits in the muon chambers with respect to the
76 linear extrapolation of the tracks from the tracking system. True muons tend to have a
77 much narrower D^2 distribution, close to zero, than the other particles that are incorrectly
78 selected by the IsMuon requirement.

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The average squared distance significance is defined as:

$$D^2 = \frac{1}{N} \sum_i \left\{ \left(\frac{x_{closest}^i - x_{track}^i}{pad_x^i} \right)^2 + \left(\frac{y_{closest}^i - y_{track}^i}{pad_y^i} \right)^2 \right\} \quad (1)$$

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where the index i runs over the fired stations, $(x_{closest,i}^i, y_{closest}^i)$ are the coordinates of the closest hit to the track extrapolation point for each station $(x_{track}^i, y_{closest}^i)$ and $pad_{x,y}^i$ correspond to one half of the pad sizes in the x,y directions.

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The D^2 distribution for muons depends on the multiple scattering and, therefore, on the momentum (p) and polar angle (θ) distributions of the analyzed sample. In order to avoid a dependence of the muon likelihood on the calibration sample (with particular p and θ), the tuning of the muon likelihood is performed separately in momentum bins and muon detector regions (which correspond to 4 intervals of θ).

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The non-muon likelihood is calibrated with the D^2 distribution for protons, since the other charged hadrons (pions or kaons) selected by IsMuon will present a D^2 distribution with a component identical to the protons and a component very similar to the true muons, due to decays in flight before the calorimeter. For protons, the hits in the muon system found around the track extrapolation are essentially due to three sources: hits from punch-through [6] protons, hits from true muons pointing to the same direction of the proton or random hits. The last two are at first order uncorrelated to the proton momentum while the first one can present some momentum dependence, less important however than the dependence expected for muons. Hence, the tuning of the non-muon likelihood is merely performed separately for the 4 muon system regions, due to their different granularity.

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The likelihood for the muon (or non-muon) hypothesis is then defined, for each candidate, as the integral of the calibrated muon (or proton) D^2 probability density function from 0 to the measured value, D_0^2 .

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The results presented in this document are obtained with a muon likelihood calibrated with muons from $J/\psi \rightarrow \mu^+ \mu^-$ decays selected from the data taken in 2010, as described in Section 4. The non-muon likelihood has been calibrated with a Monte Carlo sample of decays $\Lambda^0 \rightarrow p\pi$.

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The D^2 distributions for muons, protons, pions and kaons obtained from data are shown in the left part of Fig. 2. The distributions of the logarithm of the ratio between the muon and non-muon hypotheses (muDLL) are shown in the right panel of Fig. 2. More details about the selection of the particles used to make these plots and to extract the performance are given in Section 4.

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3.3 Combined likelihoods

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The muon and non-muon likelihoods presented in Section 3.2 can be combined with the likelihoods provided by the RICH systems and the calorimeters to improve the muon identification performance.

115 The Cherenkov angles measured in the two RICH detectors are combined with the
 116 track momentum using an overall event log-likelihood algorithm. For each track in the
 117 event, a likelihood is assigned to each of the different mass hypotheses (electron, muon,
 118 pion, kaon and proton). The RICH likelihood can differentiate between muon and other
 119 particles in particular at low momentum, below 5 GeV/c [7].

120 The energy deposition in the calorimeters also allows the evaluation of likelihoods for
 121 the muon (minimum ionizing particle), electron and hadron hypotheses [8].

122 A combined log-likelihood is then obtained for each track and for each of the different
 123 mass hypotheses by summing the logarithms of the likelihoods obtained using the muon
 124 system, the RICH and the calorimeters. In this computation, the non-muon likelihood
 125 obtained in the muon system is assigned to the electron, pion, kaon and proton hypothe-
 126 ses. The difference of the combined log-likelihoods for the muon and pion hypotheses
 127 (combined DLL) is then used to identify the muons.

128 3.4 Discriminating variable based on hits sharing

129 The number of additional tracks in the event which share hits with the muon candidate
 130 can be used to further discriminate actual muon candidates from fake ones. In order to
 131 reduce the fraction of misidentification due to nearby muons keeping a high efficiency
 132 for true muons, only additional IsMuon candidates sharing at least one hit and with a
 133 smaller D^2 value for the square distance significance are counted to build the observable
 134 called from now on N_{Shared} . Analyses which do want to reduce the probability of in-
 135 correctly identifying hadrons as muons due to this source usually select muons requiring
 136 $N_{Shared}=0$, but looser requirements are also possible, as can be seen from the N_{Shared}
 137 distributions of muons, protons, pions and kaons shown in Fig. 3.

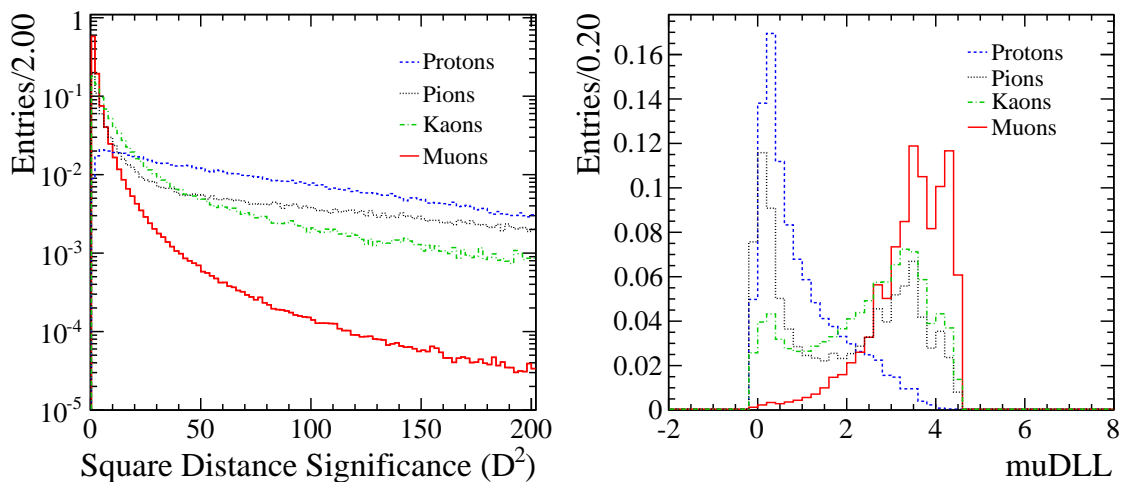


Figure 2: Average square distance distributions for muons, protons, pions and kaons (left) and the corresponding muDLL distributions (right).

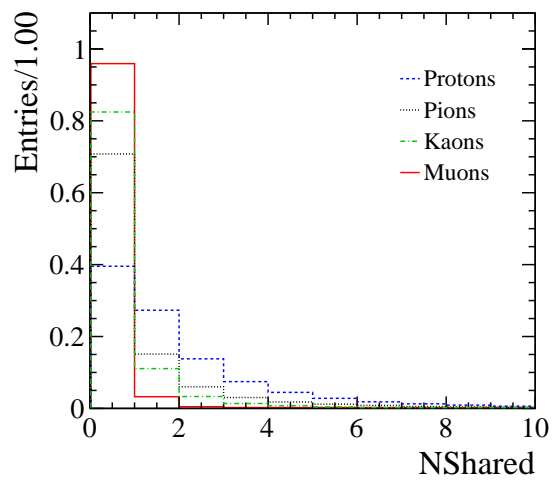


Figure 3: Normalized NShared distributions for muons, protons, kaons and pions.

4 Method for the extraction of efficiencies

In order to extract the performance of the muon identification from data, muon, proton, pion, and kaon candidates are selected with high purity from two body decays using kinematical requirements only. When necessary, the purity is improved by using a *tag and probe technique* where particle identification requirements are applied to one of the tracks (tag) while the other (probe) is used for the computation of the muon efficiency or of the hadron misidentification probability.

4.1 Selection of control samples

An abundant source of muons is provided in our experiment by the $J/\psi \rightarrow \mu^+\mu^-$ decay. By requiring the muons to have a high impact parameter with respect to the primary vertex and the reconstructed J/ψ to have a large flight distance significance and good decay vertex quality, most of the combinatorial background originating from the tracks coming from the primary vertex is removed and the sample gets enriched by $B \rightarrow J/\psi X$ candidates. In order to reduce further the combinatorial background, one of the muons is required to be identified as a muon. This is defined as the *tag* muon, while the one being probed is only required to have $p_T > 0.8 \text{ GeV}/c$.

Protons are selected from the $\Lambda^0 \rightarrow p\pi$ decays reconstructed using decay vertex quality criteria and detachment of the decay vertex from the primary one. Besides, the invariant mass obtained by assigning the π mass to the two daughters is required to be out of a window of $20 \text{ MeV}/c^2$ around the nominal K_s^0 mass.

The $D^{*+} \rightarrow \pi^+ D^0$ ($\rightarrow K^- \pi^+$) decays are our source of pions and kaons. Once again relatively high impact parameter is required for the daughters while the D^0 flight direction is required to point to the primary vertex. To evaluate the pion misidentification probability, the tag kaon is selected using a suitable cut on the π - K log-likelihoods difference, based on the RICH information. To evaluate the kaon misidentification probability, we use as well the RICH particle identification to identify the pion. Quality criteria are used for the D^{*+} and D^0 decay vertices. A window of $25 \text{ MeV}/c^2$ around the nominal D^0 mass is used to exclude the doubly Cabibbo suppressed mode and the K^+K^- and $\pi^+\pi^-$ decay channels.

To avoid our results to be biased by the trigger requirements, in the J/ψ and Λ^0 samples only events triggered independently on the probe track are used; this condition has to be satisfied at both hardware and software level, as explained in [9]. For the $D^0 \rightarrow K^- \pi^+$ sample, a substantial fraction of the events would be lost by such requirement. We therefore require that the hardware trigger fires independently on the probe track (kaon or pion) and with a software trigger decision based on impact parameter and detachment from the primary vertex only, with no particle identification requirement.

After the background subtraction of selected two-body decays, the number of muon, proton, pion and kaon candidates in the 2011 data samples are 2.4, 16.1, 11.7 and 12.3 millions, respectively.

177 4.2 Efficiency evaluation

As a baseline method to evaluate the efficiency ϵ_{muonID} of a generic muon identification requirement denoted in this section by $muonID$ (e.g. IsMuon true or DLL greater than a given cut), we use :

$$\epsilon_{muonID} = \frac{S_{true}}{S_{true} + S_{false}}, \quad (2)$$

where S_{true} and S_{false} are the numbers of signal events satisfying and not satisfying $muonID$, extracted from data using

$$S_{true,false} = N_{true,false} - B_{true,false}. \quad (3)$$

178 $N_{true,false}$ are obtained by counting the number of J/ψ candidates with invariant mass
 179 lying within a signal mass window around the J/ψ mass; the number of background
 180 events within the same mass window, $B_{true,false}$, is computed by extrapolating to the
 181 signal window the mass fit done in the J/ψ sidebands.

182 For the proton misidentification probability, the same method is used.

183 The kaon and pion misidentification probabilities are also obtained with Eq. 2, but
 184 $S_{true,false}$ and $B_{true,false}$ are extracted directly from a full fit of the signal and background
 185 shapes to the invariant mass distribution of the D^0 candidates.

186 5 Results

187 The muon identification performance is presented in terms of the muon efficiency and
 188 hadron misidentification probabilities for the different requirements. In all cases, the
 189 performance is evaluated for tracks extrapolated within the geometrical acceptance of the
 190 muon detector.

191 5.1 IsMuon performance

192 The efficiency of the IsMuon requirement, ϵ_{IM} , is the efficiency of finding hits within
 193 the fields of interest in the muon chambers for tracks extrapolated to the muon system.
 194 In Fig. 4, ϵ_{IM} is shown as a function of the muon momentum, for different transverse
 195 momentum ranges. A weak dependency with transverse momentum is observed and in
 196 particular a drop of $\sim 2\%$ is measured for the lowest p_T interval. This efficiency drop is
 197 essentially due to tracks close to the inner edges of region R1 which in principle have their
 198 extrapolation points within M1 and M5 acceptance, but are in fact scattered outside the
 199 detector. For particles with p_T above 1.7 GeV/c, the efficiency is above 97% in the whole
 200 momentum range, from 3 GeV/c to 100 GeV/c. The average efficiency obtained for the
 201 μ_{probe} in the J/ψ calibration sample is $\epsilon_{IM} = (98.13 \pm 0.04)\%$.

202 The misidentification probabilities $\wp_{IM}(p \rightarrow \mu)$, $\wp_{IM}(\pi \rightarrow \mu)$ and $\wp_{IM}(K \rightarrow \mu)$ are
 203 also shown in Fig. 4. The observed decrease of \wp_{IM} with increasing transverse momentum
 204 is expected, since tracks with higher transverse momentum traverse the detector at higher

205 polar angles, in the lower occupancy regions. The proton misidentification probability is
 206 $\lesssim 0.5\%$ for all p_T ranges and momentum above 30 GeV/c. It drops quickly with momen-
 207 tum for the lowest p_T ranges, reaching a plateau at about 30-40 GeV/c. The pion and
 208 kaon misidentification probabilities have a similar behavior, increasing with decreasing
 209 p_T . Above 40 GeV/c, the pion misidentification probability is almost at the level of the
 210 proton misidentification probability. At low momentum, decays in flight are the dominant
 211 source of incorrect identification, as can be seen from the difference between the pion/kaon
 212 and proton curves. While the proton misidentification probability, within the p_T intervals
 213 chosen, lies within 0.1-1.3%, the pion and kaon misidentification probabilities are within
 214 0.2-5.6% and 0.6-4.5%, respectively. For momentum above 30 GeV/c, $\varphi_{IM}(\pi \rightarrow \mu)$ and

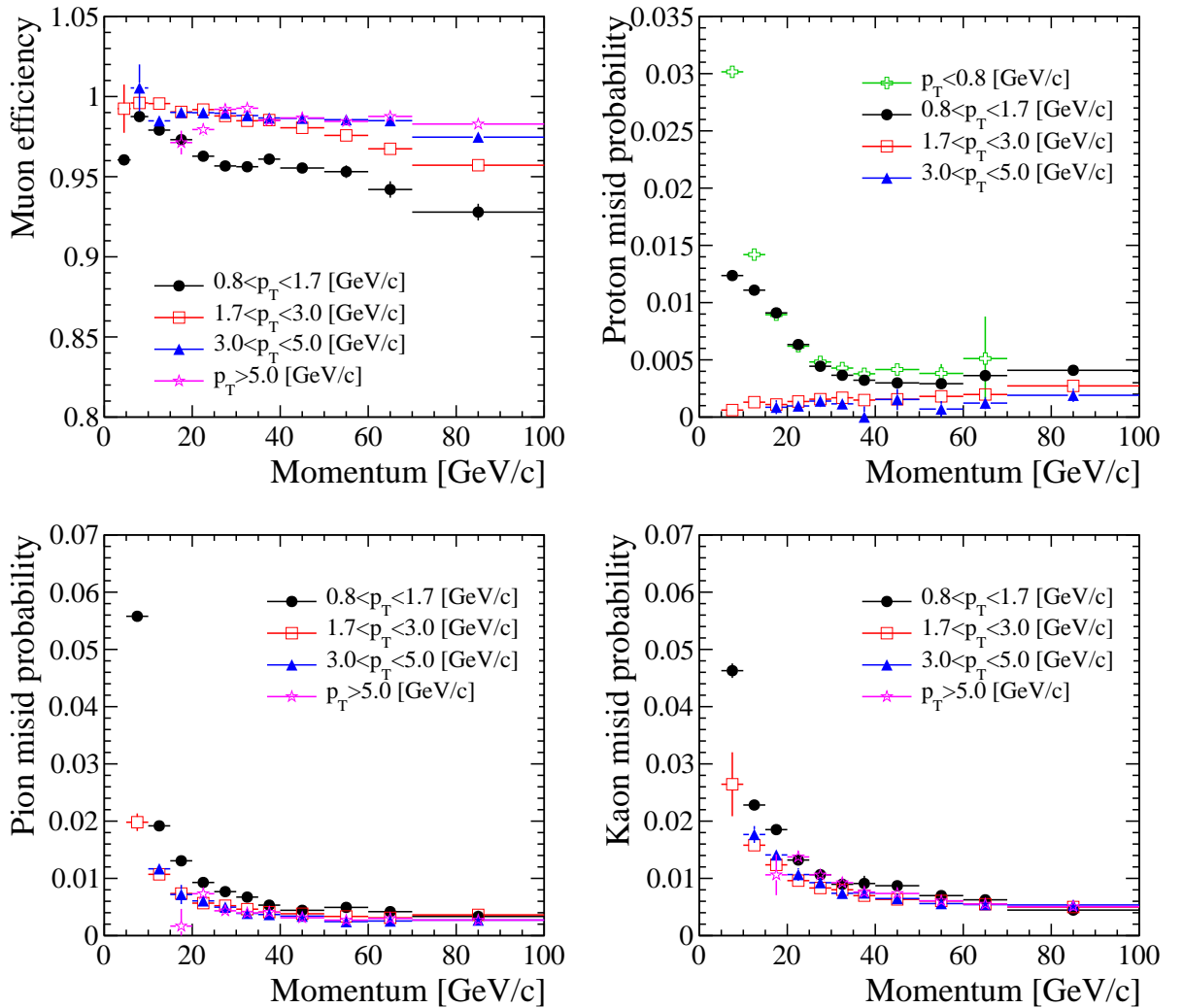


Figure 4: IsMuon efficiency and misidentification probabilities, as a function of momen-
 tum, in ranges of transverse momentum: ε_{IM} on the top left, $\varphi_{IM}(p \rightarrow \mu)$ on the top
 right, $\varphi_{IM}(\pi \rightarrow \mu)$ on the bottom left and $\varphi_{IM}(K \rightarrow \mu)$ on the bottom right.

Table 2: Average IsMuon efficiency and misid probabilities in different transverse momentum intervals (%).

p_T interval (GeV/c)	muon	proton	pion	kaon
$p_T < 0.8$		1.393 ± 0.005	6.2 ± 0.1	4.3 ± 0.1
$0.8 < p_T < 1.7$	96.94 ± 0.07	0.737 ± 0.003	2.19 ± 0.01	1.93 ± 0.1
$1.7 < p_T < 3.0$	98.53 ± 0.05	0.149 ± 0.004	0.61 ± 0.01	0.93 ± 0.01
$3.0 < p_T < 5.0$	98.51 ± 0.06	0.12 ± 0.02	0.40 ± 0.01	0.72 ± 0.01
$5.0 < p_T$	98.51 ± 0.07		0.33 ± 0.02	0.69 ± 0.01

215 $\wp_{IM}(K \rightarrow \mu)$ are practically independent of p_T . At the lowest p_T range, the kaon
 216 misidentification probability is lower than the pion for the lowest momentum interval,
 217 in spite of the larger decay width of kaons to muons. Since the muon is produced with a
 218 larger opening angle with respect to the original track trajectory in kaon decays than in
 219 pion decays and in average low momentum particles decay more upstream of the detector,
 220 then the hits in the muons chambers have a higher probability to lie outside the fields of
 221 interest.

222 When integrated over the whole p and p_T spectra of our calibration samples, the av-
 223 erage values for the misidentification probabilities are $\wp_{IM}(p \rightarrow \mu) = (1.033 \pm 0.003)\%$,
 224 $\wp_{IM}(\pi \rightarrow \mu) = (1.025 \pm 0.003)\%$ and $\wp_{IM}(K \rightarrow \mu) = (1.111 \pm 0.003)\%$. For pions and kaons,
 225 about 60% of the misidentification probability is due to decays in flight, for these partic-
 226 ular samples. The average efficiency and misid probabilities, integrated over momentum,
 227 are also given in Table 2, for 5 different p_T intervals. There aren't enough candidates
 228 in the muon, pion and kaon samples for a measurement dependent on momentum in the
 229 lowest p_T bin. Similarly for the protons, in the highest p_T interval.

230 The LHCb detector has been designed to operate at the luminosity of $\mathcal{L} = 2 \times 10^{32}$
 231 cm^2s^{-1} , at which the probability of having one interaction per beam crossing is maximal
 232 with respect to higher numbers. However, in the 2011 run the experiment operated in
 233 a much higher multiplicity environment than previously anticipated. The behavior of
 234 ε_{IM} and \wp_{IM} was then evaluated as a function of the number of tracks which contain hits
 235 in the tracking subsystems, from the VELO to the tracking stations, as those shown in the
 236 event display of Fig. 1. No significant decrease of ε_{IM} is observed while, as expected, an in-
 237 crease of the misidentification probabilities is seen. The probability $\wp_{IM}(p \rightarrow \mu)$ increases
 238 by a factor 2.7 for particles with momentum in the range 3 to 5 GeV/c, when comparing
 239 events with track multiplicity smaller than 40 and events with track multiplicity between
 240 150 and 250, which is the highest interval of multiplicity analysed. At high momentum,
 241 the difference is much less important. For pions and kaons, the increase at low momentum
 242 is around 2 and drops very quickly, becoming insignificant already at 20 GeV/c. Since the
 243 FOI are smaller at high momentum, the misidentification probability becomes less sensi-
 244 tive to the multiplicity of the underlying event. The detailed behaviour as a function of
 245 momentum is shown in Fig. 5.

246 The efficiency ε_{IM} was also analysed separately for the opposite charge muons; no

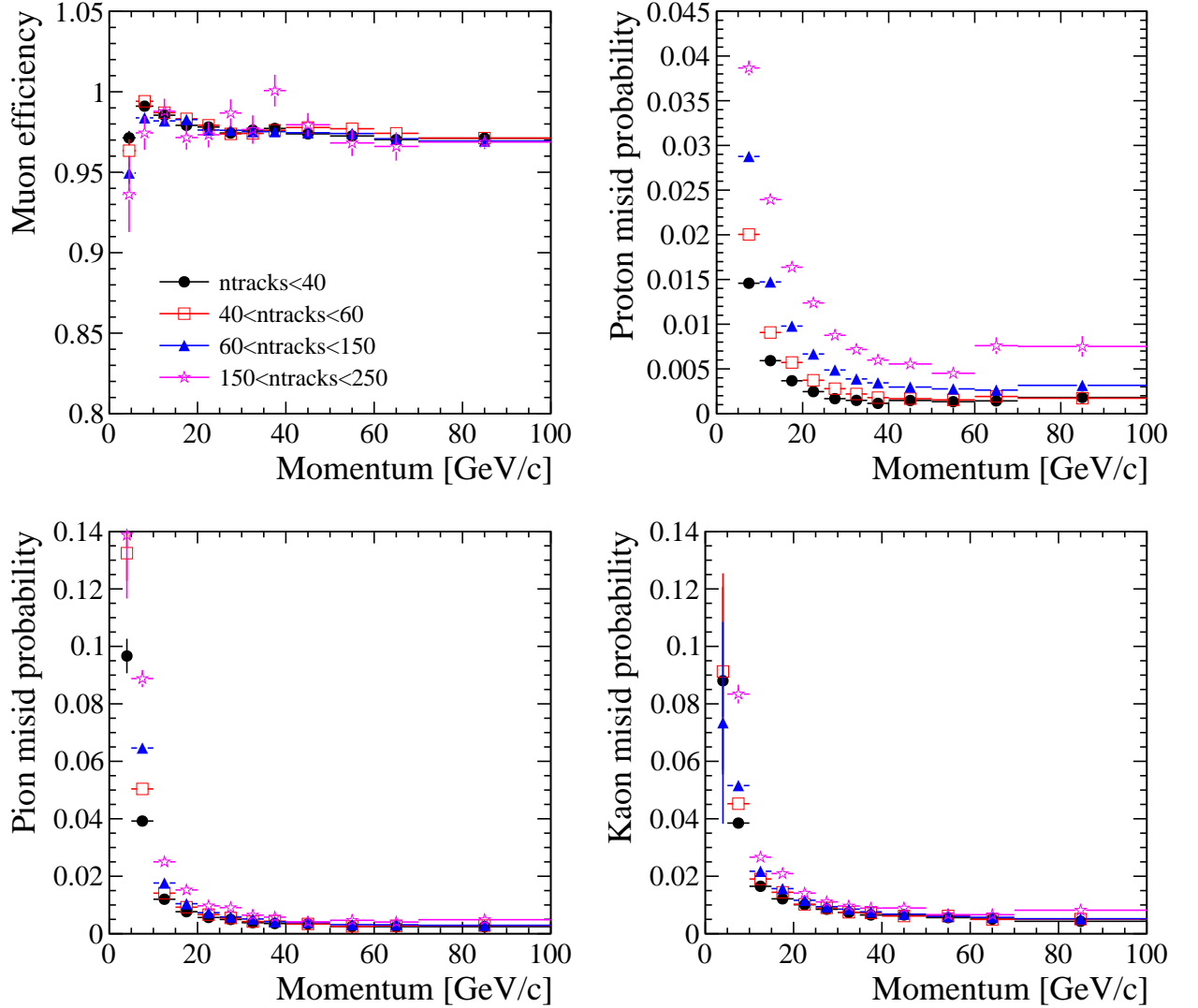


Figure 5: IsMuon efficiency ε_{IM} (top left) and \wp_{IM} for protons (top right), pions (bottom left) and kaons (bottom right) as a function of momentum for different ranges of the number of trajectories reconstructed in the event (ntracks).

247 difference between the efficiencies is seen up to the level of the statistical fluctuations.
 248 When integrating over the whole momentum range, the relative difference is $0.09 \pm 0.08\%$,
 249 compatible with zero within the statistical uncertainty.

250 5.2 Muon likelihoods

251 The muon identification efficiency ($\varepsilon_{\text{muDLL}}$) is measured as a function of a selection cut in
 252 the variable muDLL, for different momentum ranges, as shown in the top left part of Fig. 6.
 253 The misidentification probabilities are also shown in Fig. 6, for the same momentum

254 ranges. The black solid line shows the average fractions, when integrated over the whole
 255 momentum range. All the curves start at the efficiency or misidentification probability
 256 corresponding to the IsMuon requirement. The muon efficiency is independent of momen-
 257 tum up to $\text{muDLL} \sim 2$ and for tracks with $p > 10 \text{ GeV}/c$. To achieve a misidentification
 258 probability independent from the momentum, the value of the muDLL cut must depend
 259 on particle momentum. By applying a muDLL cut irrespective of the momentum, the
 260 misidentification probabilities show a strong momentum dependence.

261 As an example, requiring $\text{muDLL} \geq 1.74$, a cut that provides a muon efficiency of 95%
 262 with respect to the IsMuon efficiency (final muon efficiency of 93.2%), we obtain as final
 263 misidentification probabilities the values 0.21%, 0.78% and 0.52% for protons, kaons and
 264 pions respectively. These average values are given for our calibration samples, which
 265 have their particular momentum and p_T spectrum and will be different for samples with
 266 different kinematic distributions.

267 The momentum dependence of $\varepsilon_{\text{muDLL}}$ and of φ_{muDLL} for particles satisfying this cut
 268 are shown in Fig. 7, compared to the IsMuon requirement alone and a tighter cut,
 269 $\text{muDLL} \geq 2.25$, which reduces the muon efficiency to 90% of the IsMuon efficiency. Again,
 270 since the performance is integrated over p_T , small variations from these values are ex-
 271 pected for different samples, in particular for the misidentification probabilities, which
 272 present a stronger dependence with transverse momentum.

273 5.3 Combined likelihoods

274 The combined DLL efficiency is shown as a function of the proton, kaon and pion
 275 misidentification probabilities in Fig. 8, together with the results obtained using the
 276 muDLL alone, allowing for a direct comparison of their performances.

277 The combined DLL and muDLL alone have almost the same effect on discriminating
 278 protons from muons, while the combined DLL benefits from RICH and calorimeter infor-
 279 mation, being more effective than the muon DLL alone in separating pions and kaons from
 280 muons. In particular, the average misidentification rates corresponding to a cut which
 281 provides an average efficiency of 93.2% (equivalent to the one obtained with $\text{muDLL} \geq 1.74$,
 282 as previously shown) are around 0.22%, 0.65% and 0.38% for the protons, kaons and pions,
 283 respectively.

284 5.4 NShared performance

285 As mentioned in Section 3, after requiring IsMuon, an additional way of reducing the
 286 incorrect identification probability of hadrons as muons, in particular at high occupancy,
 287 is the use of a cut on NShared.

288 The muon efficiency is shown as a function of the pion misidentification probability
 289 for corresponding NShared cut in Fig. 9; protons are shown in the right panel of the same
 290 figure. Due to similar decay-in-flight pollution at low momentum, kaons behave as pions.
 291 The black solid line shows the average values integrated over $p > 3 \text{ GeV}/c$. The blue
 292 dotted line correspond to particles in the range $3 < p < 10 \text{ GeV}/c$. The red dashed lines

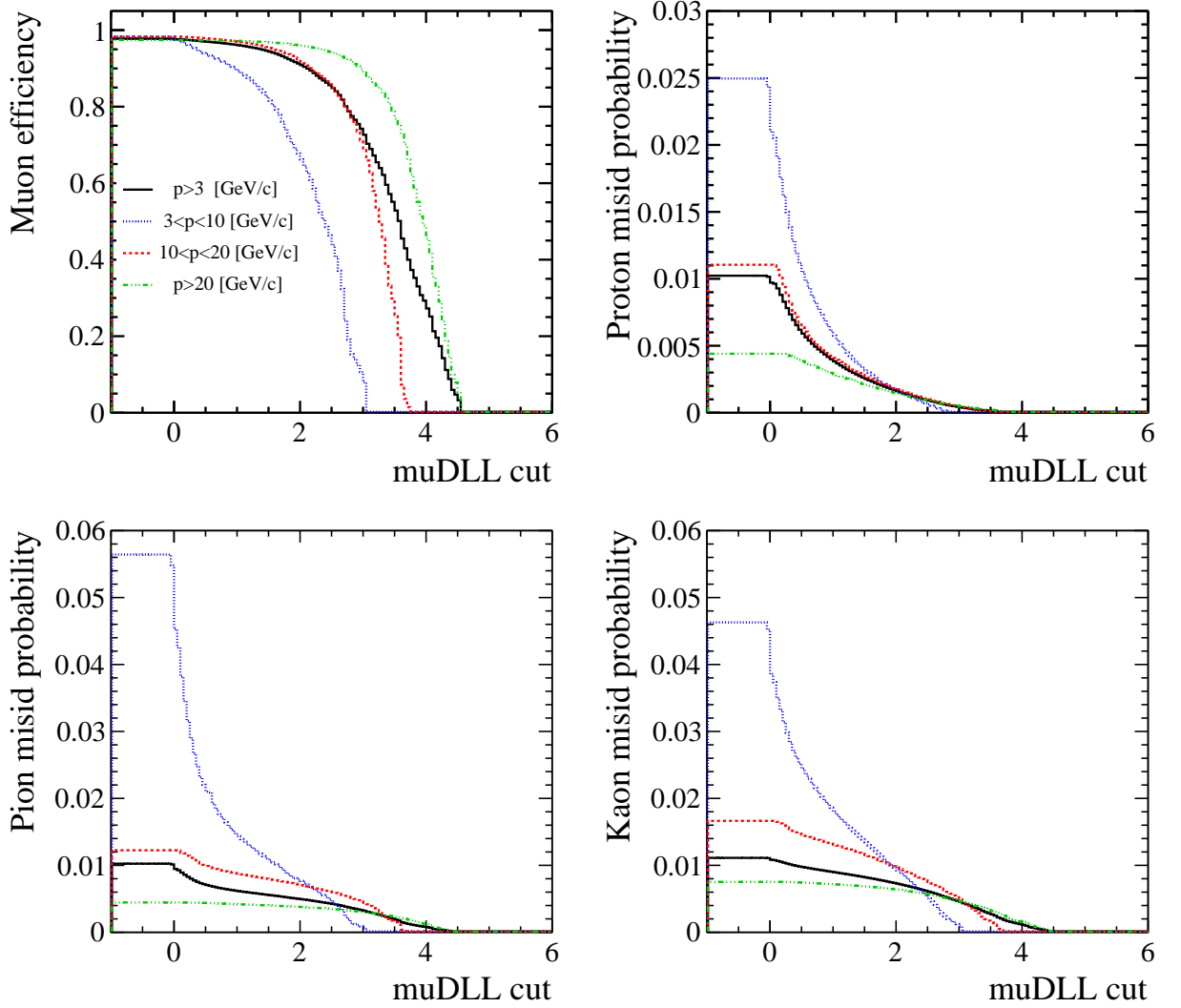


Figure 6: The efficiency $\varepsilon_{\text{muDLL}}$ as a function of muon DLL cut for muons (top left) and misidentification probabilities for protons (top right), pions (bottom left) and kaons (bottom right). The black solid line shows the average values integrated over $p > 3$ GeV/c. The blue dotted line correspond to particles in the range $3 < p < 10$ GeV/c. The red dashed lines show results for $10 < p < 20$ GeV/c and the green dashed-dotted for $p > 20$ GeV/c.

293 show results for $10 < p < 20$ GeV/c and the green dashed-dotted for $p > 20$ GeV/c. The
 294 NShared selection is particularly effective at low momenta, with increasing the FOI size.

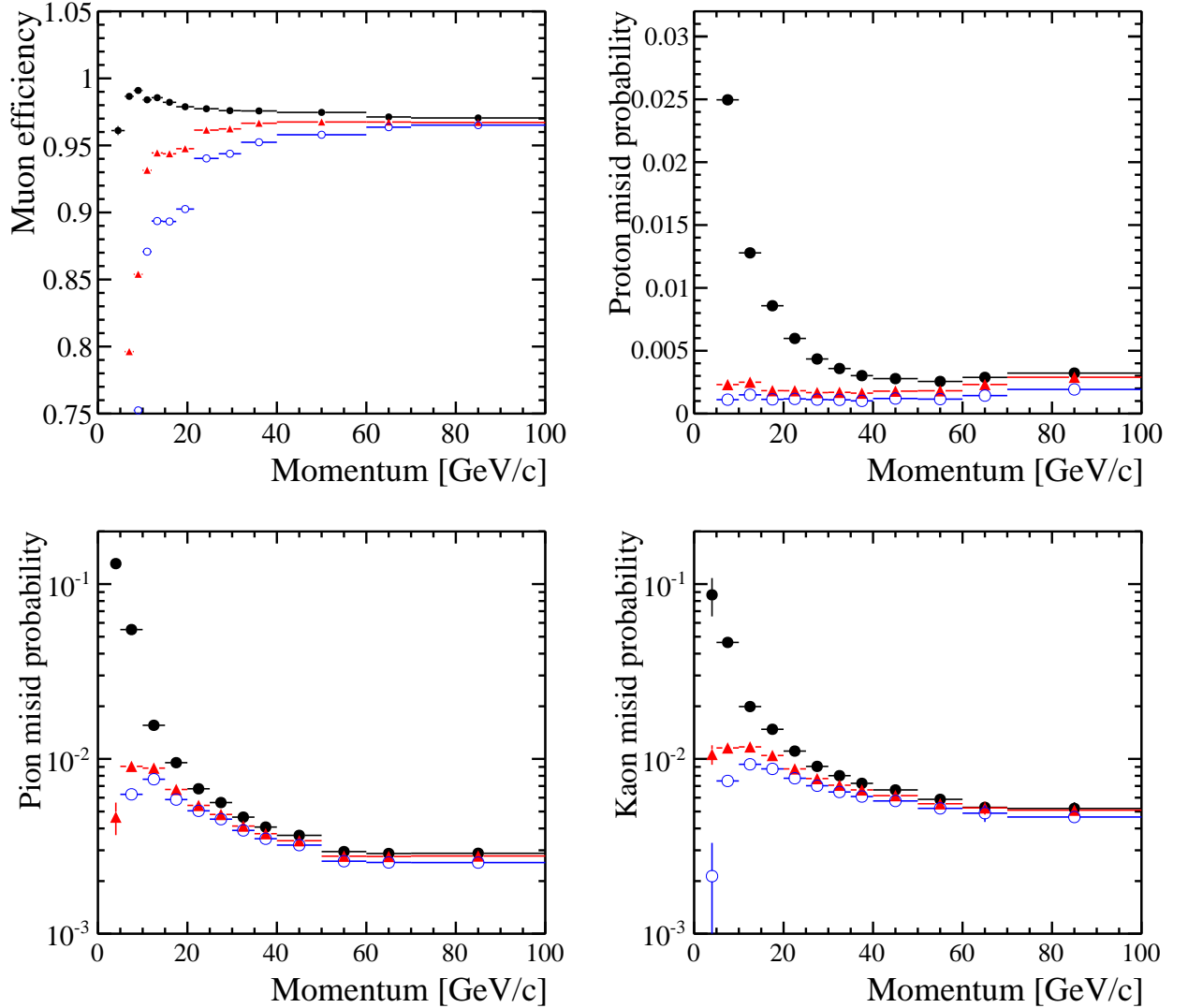


Figure 7: Muon efficiency (top left) and misidentification probabilities for protons (top right), kaons (bottom left) and pions (bottom right) as a function of the particle momentum for the IsMuon requirement alone (black solid circles) and with the additional cuts $\mu\text{DLL} \geq 1.74$ (red triangles) and $\mu\text{DLL} \geq 2.25$ (blue open circles).

5.5 Systematic checks

The effect of the trigger and of the method chosen to evaluate the efficiency and misidentification probabilities were investigated.

Alternatively to the requirement of the $J/\psi \rightarrow \mu^+ \mu^-$ sample being triggered independently of the probe muon, a muon trigger decision based on the tag muon was used to evaluate the IsMuon efficiency. The systematic uncertainty due to the choice of trigger strategy was taken as the difference between the two determinations, which is 0.2%.

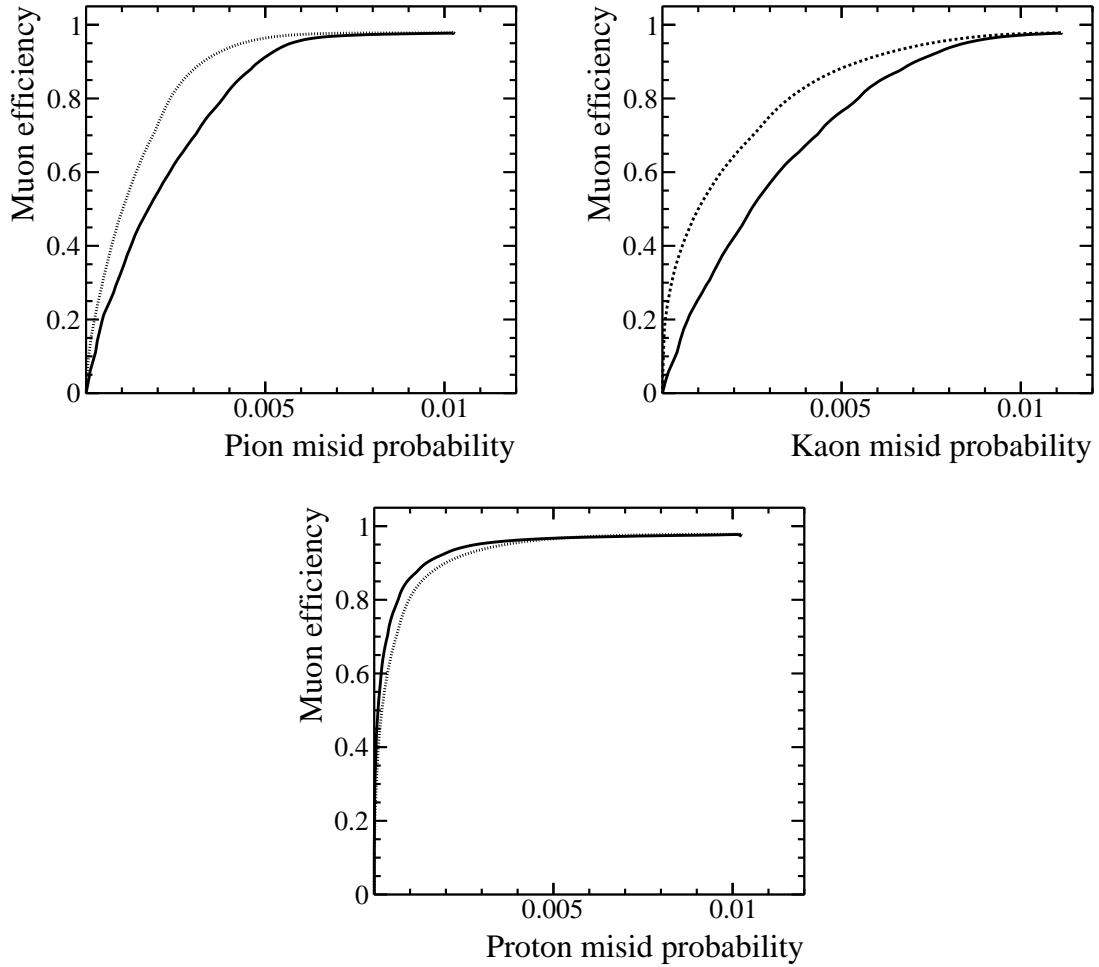


Figure 8: Average efficiency ε_{DLL} as a function of the pion (top left), kaon (top right) and proton misidentification probabilities for particles with momentum in the range $p > 3$ GeV/ c . The dotted lines show the combined DLL performance, while the muon DLL performance is shown with a solid line.

302 When performing a full fit to the signal and background components of the mass
 303 distributions used to extract the yields of signal events satisfying or not the muon iden-
 304 tification requirements, the resulting efficiencies and proton misidentification probability
 305 rates agree within the statistical uncertainties with the results shown in Section 5.

306 For the pion and kaon misidentification probabilities, the effect of the trigger was
 307 studied and found to be negligible within the errors, as shown in Fig. 10 by the constant
 308 ratio between two trigger strategies. Also the systematic uncertainty related to the method
 309 used for the evaluation of the efficiency has been studied and found to be negligible apart
 310 a few bins where it is comparable with the statistical accuracy.

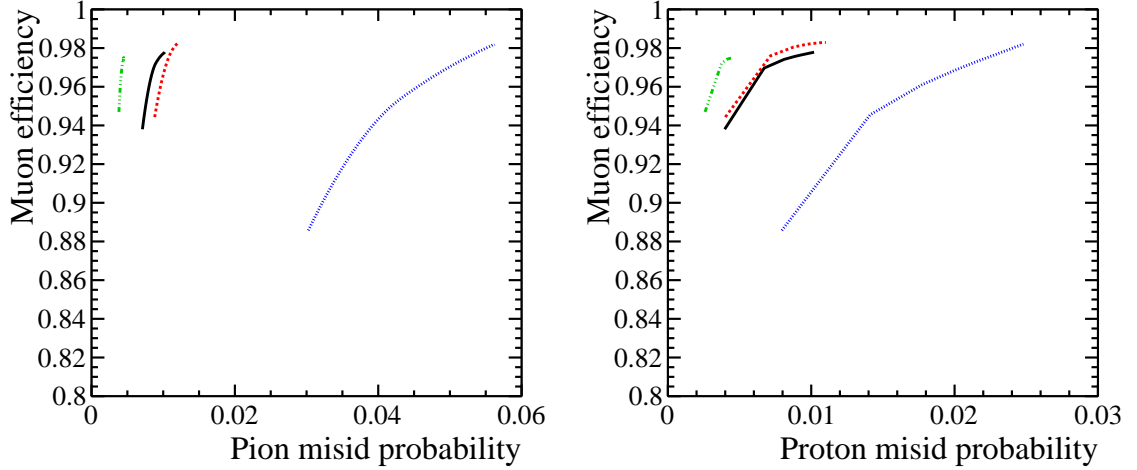


Figure 9: Efficiency $\varepsilon_{\text{NShared}}$ as a function of the pion and proton misidentification probabilities, for all particles with $p > 3 \text{ GeV}/c$ (black line) and for different momentum ranges separately: $3 < p < 10 \text{ GeV}/c$ (blue dotted), $10 < p < 20 \text{ GeV}/c$ (red dashed) and $p > 20 \text{ GeV}/c$ (green dashed-dotted).

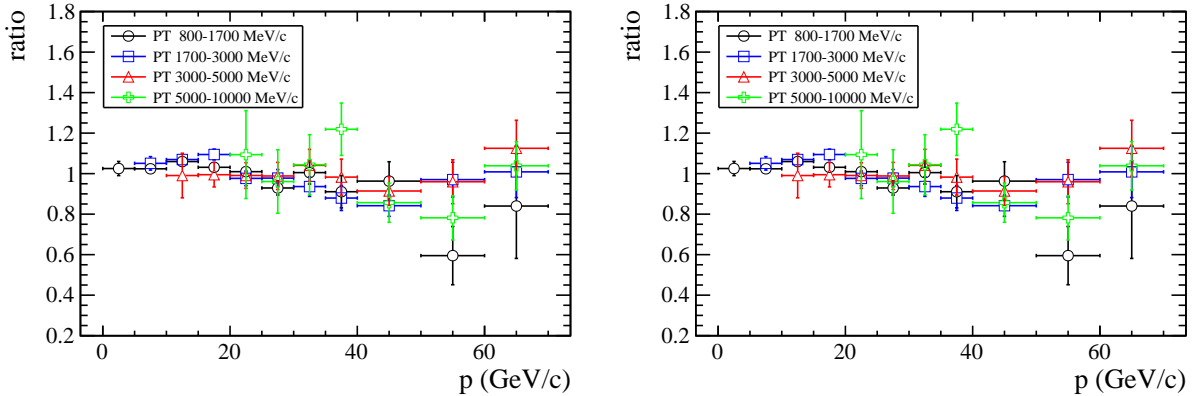


Figure 10: (a) Ratio between $\varphi_{IM}(\pi \rightarrow \mu)$ obtained with the baseline trigger requirement and a trigger independent of the pion. (b) Same for the kaon. The ratios are given as a function of momentum and transverse momentum.

311 6 Conclusions

312 We have measured the performance of the offline muon identification procedure used in
 313 the LHCb experiment, using 1 fb^{-1} of data taken in 2011.

314 The algorithm is based on a binary selection based on the matching of muon hits with
 315 the particle trajectory. For candidates satisfying this requirement, likelihoods for muon
 316 and non-muon hypotheses are built with the pattern of hits around the trajectories, which
 317 can be used to refine the selection. An additional way of rejecting fake muon candidates

318 is provided by a variable sensitive to hit sharing by nearby particles.

319 The muon identification efficiency was observed to be robust against the variation
320 of detector occupancies and presents a weak dependence on momentum and transverse
321 momentum. Hadron misidentification probabilities present a stronger dependence on hit
322 or track multiplicity, however the highest increase factors are observed only for low mo-
323 mentum particles.

324 Average muon identification efficiencies at the 98% level are attainable for pion and
325 kaon misidentification below the 1% level at high transverse momentum, using the loosest
326 identification criterium. The performance of additional requirements based on likelihoods
327 or on hits sharing can be tuned according to the needs of each analysis and reduce the
328 misidentification probabilities dependence on track multiplicity.

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